

# Limitation of time promotes cooperation in temporal games

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1 **Temporal networks are obtained from time-dependent interactions**  
2 **between individuals. The interaction can be an email, a phone call,**  
3 **a face-to-face meeting, or a collaboration. We propose a temporal**  
4 **game framework where interactions between rational individuals**  
5 **are embedded into two-player games with a time-dependent aspect**  
6 **of interaction. This allows studying the time-dependent complexity**  
7 **and variability of interactions and how they affect prosocial behav-**  
8 **ior. Based on a simple mathematical model, we find that the level**  
9 **of cooperation is promoted when the time of collaboration is limited**  
10 **and identical for every individual. We confirm and validate this with a**  
11 **series of systematic human experiments that forms a foundation for**  
12 **comprehensively describing human temporal interactions in collabora-**  
13 **tive environments. Our research reveals an important incentive**  
14 **for human cooperation, and it lays the foundations for better under-**  
15 **standing this fascinating aspect of our nature in realistic social set-**  
16 **tings.**

temporal networks | non-cooperative game | human subjects | cooperation

1 **M**any complex collaborative systems in nature, society,  
2 and engineering can be modeled through networks. In a  
3 network, nodes represent collaborating individuals, and links  
4 represent their friendships (1). In the early stage of network  
5 modeling, links are simplified to be weightless, undirected,  
6 and static. In order to improve the ability to depict real  
7 systems, weighted (2), directed (3), and dynamic (4) network  
8 models have been put forward successively. The application  
9 of these network models in various fields has fully proved  
10 that the closer the framework is to reality, the stronger its  
11 ability to explain behaviors. As an intriguing behavior in  
12 human collaborative systems, the emergence of cooperation  
13 has attracted researchers from social and natural sciences for  
14 half a century (5–8). Although we are certainly not exempt  
15 from selfishness and the fundamental principles of Darwinian  
16 evolution, cooperation is nevertheless ubiquitous across human  
17 societies (9). While the impetus for our strong cooperative  
18 drive has been linked to the difficulties of the genus *Homo*  
19 in rearing offspring that survived and to the emergence of  
20 alloparental care (10), and to the formation of alliances in  
21 times of conflicts (11), it is still puzzling as to why we have, as a  
22 species, achieved such high levels of cooperation. Our altruistic  
23 behavior distinguishes us markedly from other mammals, and  
24 they indeed form the bedrock for our astonishing evolutionary  
25 success.

26 The studies of human cooperation in *n*-person games begin  
27 with population games, also known as mean-field games (12–  
28 14). In such a well-mixed population, cooperation can hardly

29 prevail with imitative update rules when individuals play non-  
30 cooperative games such as the prisoner's dilemma (15). If the  
31 population exhibits a relatively stable social structure, the  
32 consequence may be different (16–26) – a finding with roots  
33 in the seminal paper by Nowak and May (27), who observed  
34 clusters of cooperators on a square lattice that protected them  
35 from invading defectors. Nevertheless, social networks are  
36 seldom static. We disconnect, reconnect, and then form connec-  
37 tions with new people over time. This realization has  
38 revealed new mechanisms for cooperation that may sustain co-  
39 operative behavior under extremely adverse conditions, when  
40 the temptation to defect is high and where on static networks  
41 cooperation would long perish (28). An individual also does  
42 not interact with all his friends all the time but likely does so  
43 only occasionally.

44 To account for the above aspects, dynamic networks are  
45 studied. The implications of dynamic interaction patterns on  
46 human cooperation are indeed profound, and recent human  
47 experiments, as well as theoretical research, confirm this to the  
48 fullest (2, 29–33). It was argued, for example, that such obser-  
49 vations demonstrate the effect of reputation (4). Individuals  
50 may connect with unfamiliar individuals after browsing their  
51 gaming records while cutting the existing connections with

## Significance Statement

The coupling between temporal interactions and rational decision making can be seen everywhere in real life. But the existing theoretical framework is insufficient to explain the widespread cooperation in such temporal games. We therefore conducted a series of online game experiments, which reveal a significant correlation between the high level of cooperation among individuals and the uncertainty of reestablishing collaborative relationships over time. This correlation, on the one hand, urges us to reconsider why the dynamic nature of the networks has an impact on human cooperation, and on the other hand, highlights the aptness of temporal games to explain prosocial behavior in collaborative systems.

J.W. and Y.Z. designed the research; J.W. and Y.Z. analyzed the data; Y.Z. and G.W. organized the online experiments; J.W., Y.Z., and M.P. wrote the paper; J.G., S.Z., G.C., K.C., and M.P. reviewed and revised the paper.

The authors declare that they have no conflict of interest.

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52 unsatisfactory partners. Some may take breaking ties, instead  
 53 of performing defection, as a way to penalize defectors (29).  
 54 Interestingly, the implication of dynamic reconnection fades  
 55 out when individuals choose specific moves to play games with  
 56 their partners (4). In this light, an interesting question is  
 57 whether the dynamic reconnection is relevant to the level of  
 58 cooperation in a human collaborative system if there is a time  
 59 limit on the duration of a game? From the perspective of  
 60 biological markets (34), the dynamic reconnection in such a  
 61 system is a reallocation of collaboration time in a time-limited  
 62 collaborative environment. Is too much emphasis put on the  
 63 structure of our social networks, resulting in neglecting the  
 64 temporal aspects of our interactions? In what follows, we will  
 65 address these critical questions in detail.

66 Due to the complexity of temporal systems, using evolutionary  
 67 game theory to model individuals' collaborations is  
 68 reasonably challenging. First of all, the evolution mechanism  
 69 of a temporal system itself is complicated, difficult to describe  
 70 by a simple mathematical model. Secondly, in the temporal  
 71 games, an individual strategy involves not only the moves  
 72 in games but also the allocation of time in a round. This  
 73 openness allows individual strategies and network topologies  
 74 to co-evolve in more flexible ways than the existing dynamical  
 75 gaming networks (35, 36), which further raises the difficulty  
 76 of modeling the coupled systems.

77 In this paper, we present a temporal gaming framework  
 78 upon the structure of temporal networks (37, 38). The goal is  
 79 to test the impact of limited time on the level of cooperation in  
 80 two-player collaborative systems. Such systems are common  
 81 in reality. For instance, it typically takes a team to accomplish a  
 82 project when applying for funding. The project leader  
 83 typically would collaborate with a member to accomplish a  
 84 specific part of it. Correspondingly, the member or the leader  
 85 can also be involved in more than one project. Simultaneously,  
 86 the total number of working months for each participant is  
 87 limited and identical. In such a scenario, a temporal gaming  
 88 network is naturally composed. Admittedly, the collaboration  
 89 between two team members is closer to the stag hunt game than  
 90 the Prisoner's Dilemma (PD) game. Consider cooperation  
 91 normally dominates the collaboration system playing the stag  
 92 hunt game, one can hardly differentiate the impacts from other  
 93 mechanisms. We adopt the PD game in this paper.

94 One of our key contributions is a detailed online experiment  
 95 for the theoretical framework. We first establish a gaming  
 96 platform to implement a temporal game scenario. Next, we  
 97 test the level of cooperation on the platform in a divide and  
 98 conquer (D&C) mode (4, 42, 43), where the difference from the  
 99 settings of the existing works (23, 29, 30, 39) is the targeted  
 100 decisions. Finally, we test the level of cooperation on the  
 101 platform in a time-involved mode, where the time limitation  
 102 for individuals and targeted decisions are considered. The  
 103 reasons for adopting these mechanisms will be provided in Sec-  
 104 tion *Experimental design*. What we are looking for is whether  
 105 the limitation on time resources governs human cooperation  
 106 in the games. In what follows, we will focus on this factor.

107 To clarify the impact of the limited time, we invited 183  
 108 human subjects and designed a set of comparative online  
 109 experiments. In a match, the participants are allocated to  
 110 the nodes of pre-generated networks. We test two classes of  
 111 networks, the Barabási and Albert's scale-free network (40)  
 112 and Watts and Strogatz's small-world networks, since they are  
 113 the most well-known social network models. We show that  
 114 the limitation to the individuals' time resources statistically  
 115 promotes the participants' level of cooperation, which aligns  
 116 with the theoretical prediction presented below.

## Theoretical framework of temporal games

117  
**Temporal game model.** In a two-strategy (i.e., only two moves  
 118 are allowed) game, define  $i$ 's strategy as  $\Omega_i = \begin{pmatrix} X_i \\ 1 - X_i \end{pmatrix}$ ,  
 119 where  $X_i$  can only take 1 or 0 in each game. If  $X_i = 1$ ,  $i$  is a  
 120 cooperator denoted by  $C$ . If  $X_i = 0$ ,  $i$  is a defector denoted  
 121 by  $D$ . Take the PD game (41) for example, in the PD game,  
 122 the payoff table is a  $2 \times 2$  matrix. Given  $i$ 's strategy,  $i$ 's  
 123 payoff in the game playing with all his neighbors (denoted by  
 124  $N_i$ ) can be written as  $G_i = \Omega_i^T \begin{pmatrix} \mathcal{R} & \mathcal{S} \\ \mathcal{T} & \mathcal{P} \end{pmatrix} \sum_{j \in N_i} \Omega_j$ . In the  
 125 PD model, it gains  $\mathcal{T}$  (temptation to defect) for defecting a  
 126 cooperator,  $\mathcal{R}$  (reward for mutual cooperation) for cooperating  
 127 with a cooperator,  $\mathcal{P}$  (punishment for mutual defection) for  
 128 defecting a defector, and  $\mathcal{S}$  (sucker's payoff) for cooperating  
 129 with a defector. Normally, the four payoff values satisfy the  
 130 following inequalities:  $\mathcal{T} > \mathcal{R} > \mathcal{P} > \mathcal{S}$  and  $2\mathcal{R} > \mathcal{T} + \mathcal{S}$ . Here,  
 131  $2\mathcal{R} > \mathcal{T} + \mathcal{S}$  makes mutual cooperation the best outcome from  
 132 the perspective of the collective.

133 The temporal game model proposed in this paper is based  
 134 on the game model (42, 43) taking into account the time of  
 135 interactions. As the model is time-involved, each interaction  
 136 is assigned a specific duration. The total game time for each  
 137 individual in a round is set to be constant and the same for all  
 138 individuals to be realistic to real-life scenarios. An individual's  
 139 interactions with different partners are assumed, independent.  
 140 The payoff of the game between individuals  $i$  and  $j$  can be  
 141 written as  $s_{i,j} = \Omega_{i,j}^T \begin{pmatrix} \mathcal{R} & \mathcal{S} \\ \mathcal{T} & \mathcal{P} \end{pmatrix} \Omega_{j,i}$ . In the temporal games,  
 142 the payoff of each interaction is proportional to the time it  
 143 spans. In one round of the game, the accumulated payoff of  
 144 individual  $i$  is defined as

$$\Lambda_i = \sum_{j \in N_i} \frac{\tau_{i,j}}{\mathfrak{T}} \times s_{i,j}, \quad [1] \quad 146$$

147 where  $N_i$  is the set of  $i$ 's neighbors;  $\tau_{i,j}$  is the duration of  
 148 the interaction between individuals  $i$  and  $j$ . As shown in  
 149 Fig. 1A, let  $i$  and  $j$  be the individuals colored red and blue.  
 150 Then  $N_i = 4$  and  $\tau_{i,j} = 8$ . Notably,  $\tau_{i,j}$  should satisfy the  
 151 constraints of  $\tau_{i,j} \in [0, \mathfrak{T}]$  and  $\sum_{j \in N_i} \tau_{i,j} \leq \mathfrak{T}$ . Here,  $\mathfrak{T}$  is the  
 152 total time resource of an individual in each round, which is a  
 153 constant for all individuals in our model. In Fig. 1A,  $\mathfrak{T} = 24$ .  
 154 If individual  $i$  does not want to collaborate with  $j$ , then  $i$  will  
 155 not apply for a game with  $j$  any longer. Simultaneously,  $i$  will  
 156 reject  $j$ 's gaming request. In this case,  $\tau_{i,j}$  will be 0 as the  
 157 relation between the red and the green in Fig. 1A.

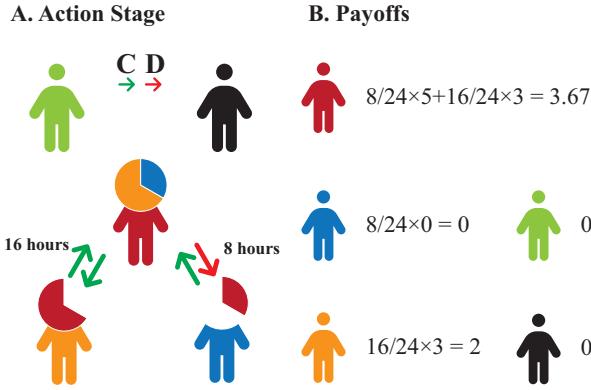
158 Let  $P_i$  be the set of partners who interacted with  $i$  in the  
 159 round, Eq. 1 can be written as

$$\Lambda_i = \sum_{j \in P_i} \frac{\tau_{i,j}}{\mathfrak{T}} \times s_{i,j}, \quad [2] \quad 160$$

161 where  $\tau_{i,j}$  is greater than 0. For the red individual in Fig. 1A,  
 162 the orange and the blue are his partners in this round. Based  
 163 on Eq. 2, the payoffs of the 5 individuals are listed in Fig. 1B.  
 164 In a mean-field view, Eq. 2 can be written as

$$\Lambda_{k_i} = \sum_{k_j} \frac{\tau_{k_i, k_j}}{\mathfrak{T}} P(k_i, k_j) s_{k_i, k_j}, \quad [3] \quad 165$$

166 where  $P(k_i, k_j)$  is the probability that a link exists between  $i$   
 167 and  $j$ , dependent on the topology of the collaborative network.



**Fig. 1.** Illustration of the temporal game. Panel A shows a round of the temporal game among 5 individuals. The individual colored red has 4 friends, in which the individuals colored orange and blue are his gaming partners. If the game between two individuals lasts for 24 hours, the payoff of a cooperator is 3 and 0, gaining from a cooperator and a defector, respectively. The payoff of a defector is 5 and 1, gaining from a cooperator and a defector, respectively.

$M_i$  to realize the update. For two players,  $i$  and  $j$ , we have

$$M_i = \begin{pmatrix} p_{CC}s_{CC} & p_{CC}(1-s_{CC}) & (1-p_{CC})s_{CC} & (1-p_{CC})(1-s_{CC}) \\ p_{CD}s_{DC} & p_{CD}(1-s_{DC}) & (1-p_{CD})s_{DC} & (1-p_{CD})(1-s_{DC}) \\ p_{DC}s_{CD} & p_{DC}(1-s_{CD}) & (1-p_{DC})s_{CD} & (1-p_{DC})(1-s_{CD}) \\ p_{DD}s_{DD} & p_{DD}(1-s_{DD}) & (1-p_{DD})s_{DD} & (1-p_{DD})(1-s_{DD}) \end{pmatrix}, \quad [4]$$

where the vectors  $\mathbf{p} = (p_{CC}, p_{CD}, p_{DC}, p_{DD})$  and  $\mathbf{s} = (s_{CC}, s_{CD}, s_{DC}, s_{DD})$  denote  $i$  and  $j$ 's probabilities of cooperation in the next round after experiencing  $CC$ ,  $CD$ ,  $DC$ , and  $DD$  cases, respectively. Then the evolution of  $i$ 's state vector  $\Phi_i(t)$  is given by

$$\Phi_i(r) = \Phi_i(r-1)M_i. \quad [5]$$

To model the the available time of individuals in the temporal games, we first assume that no players at round  $r-1$  reject the requests from an individual  $i$  if they are available. The time left for him to make use of in round  $r$  can be denoted by  $S_i(r) = \mathfrak{T} - \sum_{j \in P_i} \tau_{ujj}(r-1)$ , where  $\mu_{ij}(r-1)$  denotes the random portion of time in the request from  $i$  or  $j$  in round  $r-1$  and takes a random real number between 0 and 1. If  $i$  applies for playing with  $j$  for  $S_i(r) \mu_{ij}(r)$ , the successful probability of the request is

$$\omega_{i,j}(r, \mu_{ij}(r)) = \begin{cases} 1, & S_j(r) \geq S_i(r) \mu_{ij}(r), \\ 0, & S_j(r) < S_i(r) \mu_{ij}(r), \end{cases} \quad [6]$$

assuming  $j$  wish to play. Therefore, the expectation of difference in individual  $i$ 's available time from round  $r$  to  $r+1$  is

$$\varrho_i(r) = - \sum_{j \in N_i - P_i(r-1)} \omega_{i,j}(r, \mu_{ij}(r)) (S_i(r) - S_j(r)) \quad [7]$$

$$+ \sum_{l \in P_i(r-1)} \alpha_{il}(r-1) \left( \Phi_{il}(r) \cdot \begin{bmatrix} \chi_{i,CC} \\ \chi_{i,CD} \\ \chi_{i,DC} \\ \chi_{i,DD} \end{bmatrix} \right) \mu_{ij}(r), \quad [228]$$

where  $\chi_i$  denotes  $i$ 's probabilities of reassigning time after experiencing the four outcomes.  $\alpha_{il}(r)$  denotes the time share which  $i$  assigns to  $j$  at round  $r$ . Note that

$$\sum_{l \in P_i} \alpha_{il}(r) + S_i(r) = 1. \quad [8]$$

Considering  $S_i(r) \geq 0$  for all  $r$ , the iterative formula of  $S_i(r)$  should be written as

$$S_i(r+1) = \text{Relu}(\varrho_i(r) + S_i(r)), \quad [9]$$

where  $\text{Relu}(x) = \begin{cases} x, & x \geq 0, \\ 0, & x < 0. \end{cases}$  As the evolution procedure

of  $S_i(r)$  in the system can not be modeled in a mean-field way, one can hardly present an analytical solution to it. Therefore, we will present the simulation results and empirical results from human online experiments in the following. In the simulations, we uniformly set the agents to adopt the same strategy to have the results reproducible. Let the number of agents be  $N_A$ . We will show that the average available time  $S(r) = \frac{\sum_i S_i(r)}{N_A}$  falls to a low level at the first round. It is stabilized after then, indicating that finding new partners is problematic from the beginning of a match.

## Results

To show the impact of time redistribution, we first simulate the evolution of moves when agents play a traditional Prisoner's dilemma (PD) game with their neighbors in the BA and WS

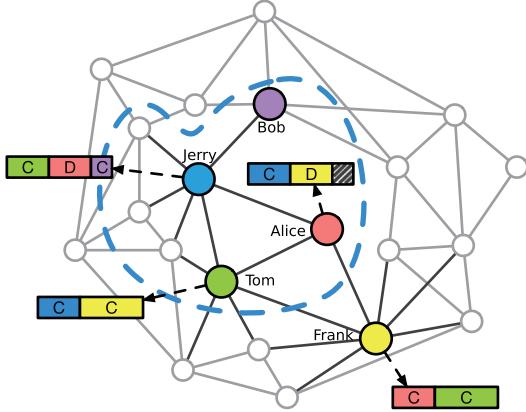
We show an illustration of such a collaborative network in Fig. 2A. To clarify the generating procedure of the network, we provide the communication log among the individuals in this round in Fig. 2B. In the log, Alice tried collaborating with Tom for  $\mathfrak{T}$ , while Tom had agreed to work with Jerry and Frank when he received Alice's request. Thus, Alice turned to Frank and Jerry, but it was a bit late to make appointments with them as they were partially engaged. As a result, Alice took  $0.8\mathfrak{T}$  to play with Frank and Jerry and wasted  $0.2\mathfrak{T}$  in this round. For a heterogeneous network as the Barabási-Albert (BA) networks (44),  $P(k_i, k_j) \sim \frac{k_j P(k_j)}{\langle k \rangle}$ . For a homogeneous networks as the Watts and Strogatz (WS) networks (45),  $P(k_i, k_j) \sim P(k_j)$ .

**Proportion of cooperation in the temporal game.** In the temporal game, each game between partners is coupled with a duration. Therefore, the level of cooperation should be measured by the duration and their moves. We define the proportion of cooperation as  $P_c = \frac{T_C}{T_G}$ , where  $T_G$  is the total duration of the moves and  $T_C$  is the total duration of cooperation in the games.

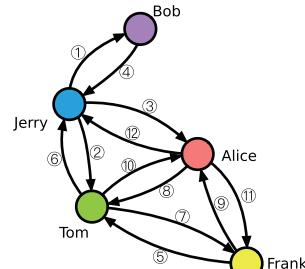
Note that current studies on decision time (46, 47) in experimental psychology and response time in experimental economics (48, 49) focus on the time of making a decision rather than the duration of moves. Therefore, the object of such studies is different from that of temporal games.

**Mathematical modeling the available time of individuals.** As is known, for each game between two players, each player has to experience one of the four possible cases, namely, cooperating with a cooperator (CC), cooperating with a defector (CD), defecting a cooperator (DC), and defecting a defector (DD). We define a state vector  $\Phi$  by  $(\Phi_{CC}, \Phi_{CD}, \Phi_{DC}, \Phi_{DD})$ , in which each entry corresponds to the probability of experiencing the respective outcome. Generally, a memory-one strategy can be written as  $\mathbf{p} = (p_{CC}, p_{CD}, p_{DC}, p_{DD})$ , corresponding to the probabilities of cooperating under each of the previous outcomes. Since players update their moves with the memory-one strategies in each time step, the update can be considered a Markov process. One can find a Markov transition matrix

A



B



Communication Log

| No. | From  | To    | Communication Records              |
|-----|-------|-------|------------------------------------|
| ①   | Jerry | Bob   | Request for interaction with 0.25. |
| ②   | Jerry | Tom   | Request for interaction with 0.45. |
| ③   | Jerry | Alice | Request for interaction with 0.45. |
| ④   | Bob   | Jerry | OK.                                |
| ⑤   | Frank | Tom   | Request for interaction with 0.65. |
| ⑥   | Tom   | Jerry | OK.                                |
| ⑦   | Tom   | Frank | OK.                                |
| ⑧   | Alice | Tom   | Request for interaction with 1.    |
| ⑨   | Frank | Alice | Request for interaction with 0.45. |
| ⑩   | Tom   | Alice | Sorry.                             |
| ⑪   | Alice | Frank | OK.                                |
| ⑫   | Alice | Jerry | OK.                                |

**Fig. 2.** Illustration of the temporal games in a two-player collaborative system. (A) One round of the temporal game on a social network. The blue circle is Jerry's neighborhood. Alice, Bob, and Tom are Jerry's partners in this round. The color of a time slot represents a partner; for instance, yellow represents Frank.  $C$  or  $D$  in the time slot denotes the move from the individual at the tail of a directed dashed line to the indicated specific partner. (B) The generating procedure of the circumstance presented in (A). In the communication log, the records are sorted by their sequence numbers in ascending order. Only if both players agree to collaborate (the response to a request is OK) will their colors appear in each other's collaboration schedule, i.e., a time slot in (A).

Table 1. The basic information of matches.

| Game Number | Game Type      | Type of Network | Number of Participants | Number of Rounds | Corresponding Panel in Fig. 4 |
|-------------|----------------|-----------------|------------------------|------------------|-------------------------------|
| G1224       | D&C            | BA              | 39                     | 13               | Fig. 4(a)                     |
| G1230       | D&C            | BA              | 17                     | 16               | Fig. 4(a)                     |
| G646        | Temporal Games | BA              | 50                     | 11               | Fig. 4(b)                     |
| G903        | Temporal Games | BA              | 44                     | 28               | Fig. 4(b)                     |
| G1228       | D&C            | WS              | 34                     | 13               | Fig. 4(c)                     |
| G1234       | D&C            | WS              | 21                     | 15               | Fig. 4(c)                     |
| G936        | Temporal Games | WS              | 22                     | 24               | Fig. 4(d)                     |
| G933        | Temporal Games | WS              | 22                     | 28               | Fig. 4(d)                     |

networks. In a network, a player starts a game with a gaming request to a neighbor. In our simulations, all the agents in the network are selected one by one, following a random sequence. For a selected agent, it evenly allocates the time left to its requests to the uncoordinated neighbors. If the requested neighbor has enough time to accept the gaming request, he will accept it. After one round of the game, agents will uniformly update their moves with the Zero-Determinant Extortionate strategy proposed in reference (57). The strategy will wipe the cooperators out in a few rounds. If an agent defects in a round, the pair will be taken apart with a certain probability. The separation means the time assigned to the pair will be redistributed next round. More details on the simulations will be provided in Section *Simulation on the social networks*.

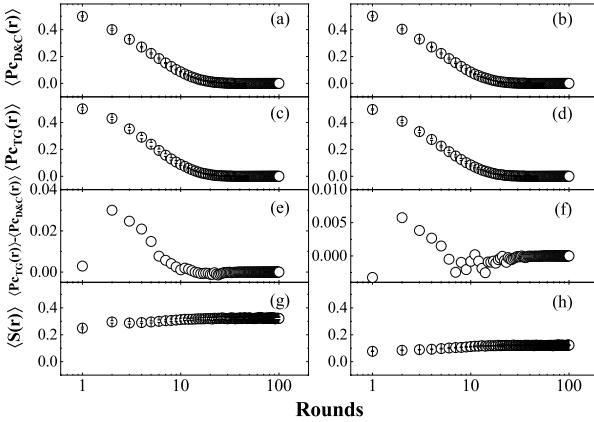
In Fig. 3(a) and 3(b), the results show the level of cooperation decays with rounds for agents playing the ‘divide-and-conquer’ (D&C) games (4, 42, 43) in both networks. After being affected by the temporal mechanisms, the rates of decay slow down in Fig. 3(c) and 3(d). We show the difference in the level of cooperation between the temporal games and the D&C games (4, 42, 43) in Fig. 3(e) and 3(f), which will be amplified when human subjects play. The amplification may originate from  $S(r)$  shown in Fig. 3(g) and 3(h), which will be much lower when humans play the temporal games.

To test the validity of our theoretical results, we invite 183 volunteers to attend 8 online experiments. For conciseness, we show the basic information of each match in Table 1. After comparing Fig. 4(a) with Fig. 4(b) and Fig. 4(c) with Fig. 4(d), one can see that the decay of  $P_c(r)$  in the temporal games is slower than that in the D&C games. The result confirms our

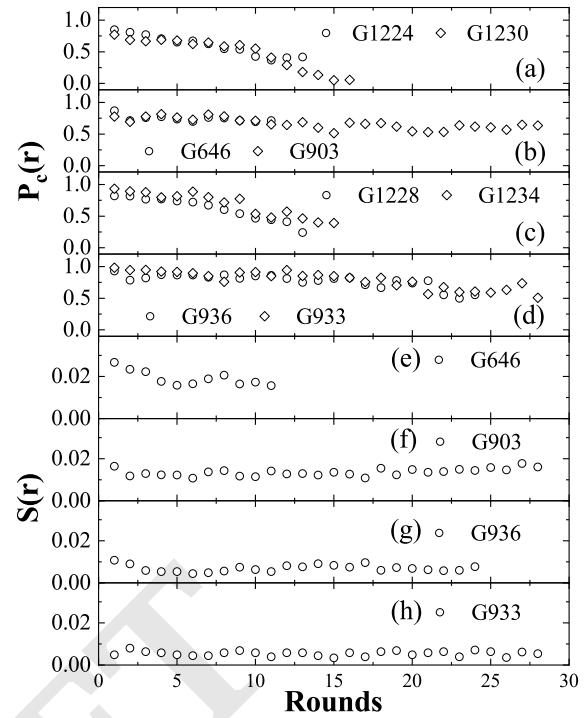
theoretical prediction, indicating the limitation on gaming time promotes the level of cooperation in gaming social networks.

To explain the behavior, we measure the average available time  $S(r)$  in the four time-involved matches. The evolution of  $S(r)$  for the two BA networks are shown in Fig. 4(e) and Fig. 4(f), respectively. The corresponding results for the two WS networks are shown in Fig. 4(g) and Fig. 4(h), respectively. One can see that  $S(r)$  fluctuates around a small positive value in the four panels, revealing the difficulty of finding new partners when humans play the temporal games is more significant than our theoretical prediction. The difference in  $P_c(r)$  between the theoretical prediction and human behavior suggests that the rising of the difficulty of finding new partners may lead to the promotion of  $P_c(r)$ , which to some extent explains why the limited time promotes the level of cooperation in a social network.

The other behavior which should be noted is that the level of cooperation generally decays with rounds in Fig. 4. The behavior is caused by the number of rounds for each match being limited, although it is random. This limitation mainly comes from the time of the subjects, since it is complicated to ask about 100 students to play online for more than an hour simultaneously, even though we pay them acceptable participation fees and provide attractive rewards for the winners of each match. We show some of the winners’ strategies in Section **Top Voted Strategies of Supplementary Information (SI)**. One can see that the level of cooperation decays when the participants guess that the match is ending.



**Fig. 3.** Evolution of the average proportion of cooperation  $\langle P_c(r) \rangle$  in the 'divide-and-conquer' (D&C) and temporal gaming networks. (a) and (c) show  $\langle P_c(r) \rangle$  of the D&C games and temporal games in the BA networks, respectively. (b) and (d) show  $\langle P_c(r) \rangle$  of the two classes of games in the WS networks, respectively. (e) and (f) show the difference of  $\langle P_c(r) \rangle$  between the D&C games and the temporal games in the BA and WS networks, respectively. Each plot denotes the average of 10 simulation runs. As the system evolves dramatically at the beginning of the experiments, we show the results in semi-log coordinates.



**Fig. 4.** Evolution of the average proportion of cooperation  $P_c(r)$  and the average proportion of cooperation  $S(r)$  in the temporal games played by human subjects. (a) and (c) show the results of the D&C games in the BA networks and WS networks, respectively. (b) and (d) show the results of the temporal games in the BA networks and WS networks, respectively. Horizontal coordinates denote the number of rounds. (e) and (f) show the results of two temporal games in the BA networks. (g) and (h) show the results of two temporal games in the WS networks.

impacting disciplines from preserving natural resources to designing institutional policies.

## Materials and Methods

**Experimental design.** In order to build an experimental environment as close as possible to natural temporal two-player collaborative systems, two realistic factors are considered in our empirical study. First, the interactive time is determined by negotiation. The setting restores the temporal property of a game in reality. A dynamic reconnection is implemented in the network by rejecting a friend's request and then proposing a game with another friend (29, 31). Second, a 'divide-and-conquer' (D&C) framework, also referred to as targeted decision, is adopted, in which the individuals who propose a game or accept a gaming request have to decide whether to cooperate (*C*) or to defect (*D*) in each round of the game (4, 42, 43). Most existing research on gaming networks is performed under a framework where individuals choose the same move to interact with all their neighbors (29–31). On the contrary, in real-world scenarios, people do not normally defect their long-term partners after being defected by other partners. In a realistic social network, they would choose a specific move to play with a partner, referred to as the D&C game in the literature (42, 43). When the diffuse decision scheme is replaced by the D&C or targeted decision scheme, the impact of dynamic reconnection on promoting cooperation will become negligible (4).

The coupling between temporal interaction and rational decision-making can be seen everywhere in real life. Still, the existing theoretical frameworks seem insufficient to explain the widespread cooperation in such temporal games. Under the framework of temporal games, we designed a series of online game experiments. With the experimental data, we present a surprising finding: limitation of time promotes cooperation in temporal games. This finding, on the one hand, urges us to reconsider how much the dynamic

## Discussion

As a theoretical framework closer to realistic scenarios, the temporal game has demonstrated its capacity to illuminate complex behaviors in our social experiment. The human behaviors revealed from the human temporal games were rarely reported previously in the literature. When the available time resources of individuals in the gaming network are scarce, the individuals are more likely to maintain the current relationships through cooperation. The underlying mechanism is that interactions are not obligated but spontaneous. If an individual's time resource cannot afford the requested duration of the interaction, he will have no choice but to abandon it, which makes it much harder to find new partners. The accordance of empirical and simulation results confirms the significance of the mechanism. Our finding reveals a fundamental reason for lasting altruistic behaviors in real human interactions, providing a novel perspective for understanding the prevailing of human cooperative behaviors in temporal collaboration systems.

Note that the limitation on time is an objective fact in human collaboration systems, which is essentially different from the incentives, such as global reputation (50, 51) and onymity (52), associated with human psychology. In a sense, the behavior observed in our experiments is more deterministic. Introducing some other mechanisms like reward (53) and costly punishment (54, 55) to the temporal systems will be a natural extension in this direction. Apart from the mechanisms, the impact from different types of games, for instance, the snowdrift game (56) and the public goods game (19), is also of particular interest.

Our work considers the temporal game framework and presents some surprising results. There are several interesting future directions, both in terms of theoretical and experimental results. However, the basic theoretical model and the key experimental results we present in this work for temporal games are the first steps to modeling realistic networks with time-dependent interactions. Such realistic modeling will allow better analysis, prediction, and design principles for the emergence of cooperation in network models, profoundly

380 nature of networks can impact human cooperation. On the other  
 381 hand, it implies the potential of the temporal game framework to  
 382 explain various collective behaviors in real two-player collaborative  
 383 systems. Our results have a profound impact on the study  
 384 of pro-social behavior. By accounting for the time-dependent aspect  
 385 to model a realistic network, we present an interesting finding  
 386 which can improve our understanding of widespread cooperation in  
 387 time-dependent collaborations.

388 **Experimental setup and game rules.** A series of online human subject  
 389 experiments were designed to build a two-player collaborative system  
 390 of rational individuals. A total of 183 human subjects participated  
 391 in 8 matches in the experiment. The majority of subjects are  
 392 students from Tongji University and Southeast University in China.  
 393 To implement the designed scenario, a novel online gaming platform  
 394 was developed, called the *War of Strategies* (<http://strategywar.net>),  
 395 see (Section **Experimental Platform and Interface of SI** for  
 396 the details of the platform).

397 In the online experiments, participants played a traditional Prisoner's  
 398 dilemma (PD) game, where  $C$  and  $D$  were the only available  
 399 actions. Each participant interacted with the individuals who had  
 400 agreements with him in one round, after which the agreements need  
 401 to be redrafted.

402 Each match on the platform comprises two stages. In the first  
 403 stage, the system generates a network with a social network model.  
 404 The subjects are then allocated to the nodes of the network. Therefore,  
 405 the connections among the subjects are randomly predetermined.  
 406 The second stage is an  $n$ -round iterated PD game, where  
 407  $10 \leq n \leq 30$  is unknown to individuals to avoid the ending-game  
 408 effects.

409 In each round of the game, individuals can make requests for  
 410 interactions with their friends. In a request, the duration of the  
 411 interaction is suggested by the sender and shown to the target.  
 412 The request can be accepted, denied, ignored, or canceled. Once  
 413 an individual accepts it, the individual has to choose a move as a  
 414 response. The payoff of the game is proportional to the duration  
 415 suggested in the request, which is a part or all of the sender's time  
 416 resource. Once the request is sent out, this part of the resource  
 417 will be occupied before receiving a response, which cannot be used  
 418 again in any other interaction. If the request is accepted, the time  
 419 resource will be consumed. If the request is denied, ignored, or  
 420 canceled, the time resource will be returned to the sender. The  
 421 total time resource assigned to each individual is 1,440 units in  
 422 each round, simulating one day in real life. We adopt 1,440 to help  
 423 the participants to understand its meaning, the value of which is  
 424 irrelevant to our results. For all the individuals, each round lasts  
 425 for 60 seconds. The initial aggregated payoff for each individual is  
 426 0. The payoff matrix is the same as that in Fig. 1.

427 During the match, the individual IDs are randomly generated.  
 428 The individuals can only see their own game records, where each  
 429 record includes the moves of both sides and the time durations.  
 430 The topological structures beyond their immediate neighbors are  
 431 invisible to them. Besides, individuals are shown their aggregated  
 432 payoff, time resources, number of rounds played, and their decision  
 433 time remaining.

434 **Simulation on the social networks.** Here, we will present the process  
 435 of the simulation. Step 1, Generate a structured population such  
 436 as the Barabási and Albert's scale-free network (40) with degree  
 437  $m_0 = m = 3$  or Watts and Strogatz's small-world network with  
 438  $P_{\text{rewire}} = 0.1$  and  $K = 6$ . Randomly assign the agents to be  
 439 cooperators with a probability of 0.5. The size of the population  
 440 is set to 1,024. Step 2, Shuffle the agent list and iteratively ask  
 441 an agent to broadcast gaming requests to its neighbors. In each  
 442 request, the agent evenly allocates its time left to its uncoordinated  
 443 neighbors, i.e.,  $\mu_{ij}(r) = \frac{1}{|N_i - P_i(r-1)|}$ , where  $j \in N_i - P_i(r-1)$ .  
 444 If a neighbor has enough time to accept the request, he will accept  
 445 it. Step 3, Each pair of the matched agents game for one round and  
 446 update their moves, following the Zero-Determinant Extortionate  
 447 strategy proposed in reference (57). Step 4, If an agent defects in  
 448 the round, the pair will be taken apart with a probability of 0.5,  
 449 that is,  $\chi = [0, 0.5, 0.5, 0.5]$ . Step 5, Repeat Steps 2, 3, and 4 until  
 450 the preset number of rounds.

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